

Signal and Information Processing

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Presentations

Data, Signals, and Information

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- ▶ My research is on **signal and information processing**. Best possible class for me to teach

- ▶ We meet online ⇒ Mondays, Wednesdays, Fridays 10 am to 11 am

- ▶ **I would like to see you in class**. A minimum level of social connection is important!

- ▶ There is ample empirical evidence on the large **correlation of grades and class attendance**

- ▶ Course's website \Rightarrow <https://ese224.seas.upenn.edu/>
- ▶ Discussion forum in Piazza \Rightarrow <https://piazza.com/class/kjuecpey9hb4hr>

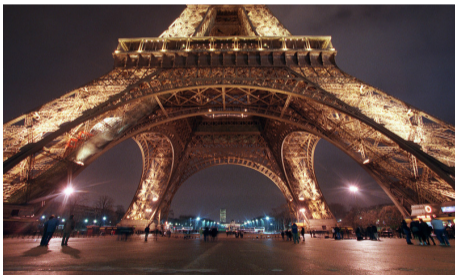
- ▶ Luana Ruiz
- ▶ Vinicius Lima
- ▶ Zhan Gao
- ▶ Zhiyang Wang
- ▶ Juan Cerviño

- ▶ First midterm will be in class, during the lecture on **Friday, March 6**
⇒ This is the Friday right before the Spring break. Plan accordingly!
- ▶ Second midterm on the **Wednesday, April 29** lecture ⇒ Worth 26 points. **Not cumulative.**
⇒ This is the last day of classes. Plan accordingly!
- ▶ You will be handing in 13 lab reports which we will grade from 0 to 4
⇒ No show (0). Poor (1). Fair (2). Good (3). Excellent (4)
- ▶ Maximum possible points: $104 = 26 + 26 + 13 \times 4$
- ▶ You **pass** with **60 points** and **13 points** in midterm and final (each)
- ▶ C requires at least 70 points. B at least 80. **A at least 90**
- ▶ Don't worry. We will work hard. We will learn. We will get A's.

Presentations

Data, Signals, and Information

- ▶ **Data and signals are collections of values** (numbers) we have acquired
⇒ A conversation recording, an image, car fuel efficiency
- ▶ People tend to say “signal” if they are electrical engineers. and to say “data” if they are not



- ▶ In any event, this disagreement is irrelevant ⇒ Signals and data are **functions**

- ▶ **Information is the answer to a question** of interest
 - ⇒ For example, these two are pictures of the Eiffel tower
 - ⇒ But also, “the tower is illuminated” (left) or “the tower is under construction (right)”

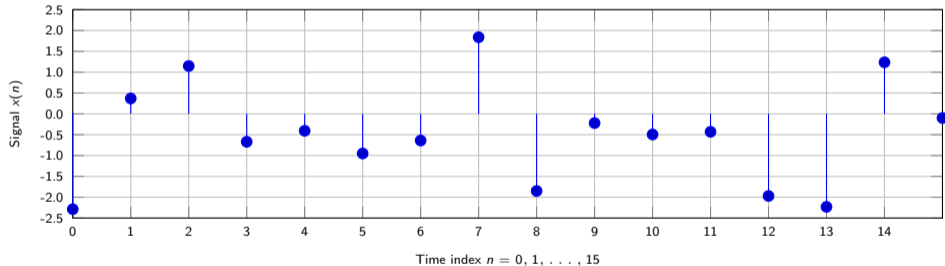


- ▶ The goal of signal processing is to **extract information from data**

- ▶ The pragmatist: Data is different from information
- ▶ The purist: Information is not created by processing ⇒ Data IS information
- ▶ I am a pragmatist, but the purist is right
- ▶ Dodo principle: Everybody has won and all must have prizes
⇒ Process signals and information to uncover patterns of interest

- ▶ What is so difficult about signal processing?

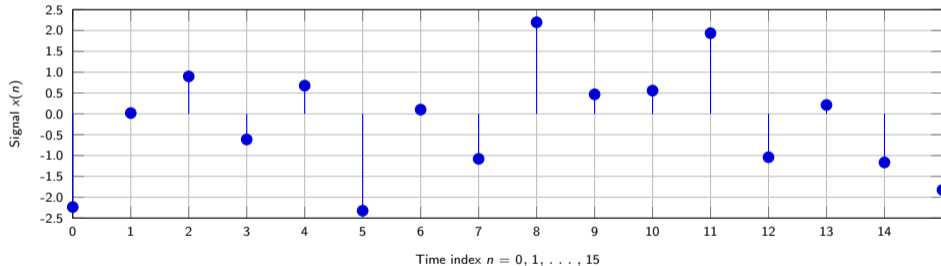
⇒ Dimensionality ⇒ The number of possible signals is too large



- ▶ This is one signal with 16 components

- ▶ What is so difficult about signal processing?

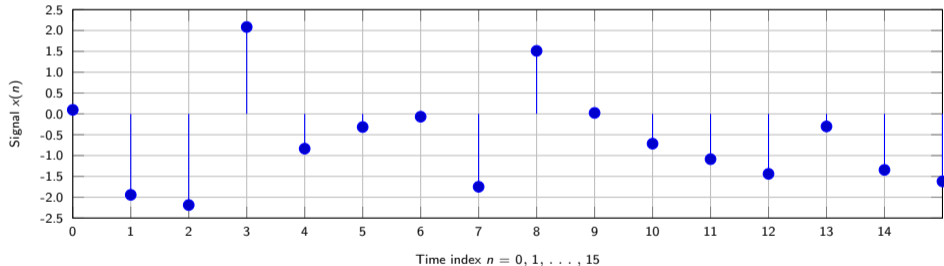
⇒ Dimensionality ⇒ The number of possible signals is too large



- ▶ This is a **second** signal with 16 components

- ▶ What is so difficult about signal processing?

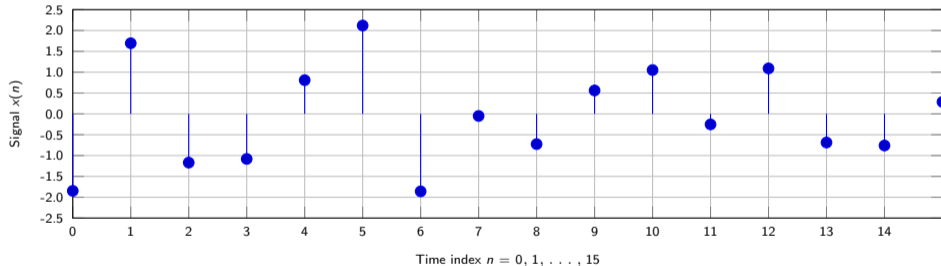
⇒ Dimensionality ⇒ The number of possible signals is too large



- ▶ This is a **third** signal with 16 components

- ▶ What is so difficult about signal processing?

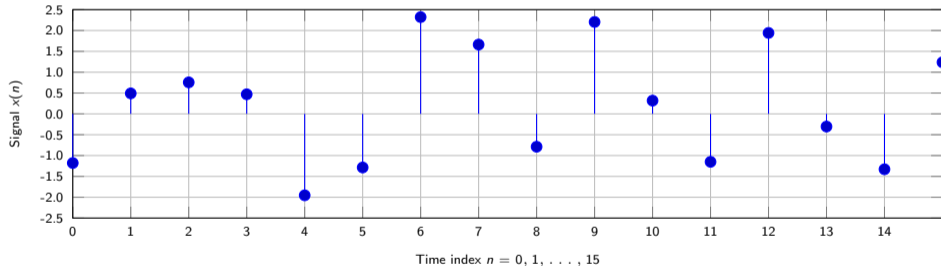
⇒ Dimensionality ⇒ The number of possible signals is too large



- ▶ This is a **fourth** signal with 16 components

- ▶ What is so difficult about signal processing?

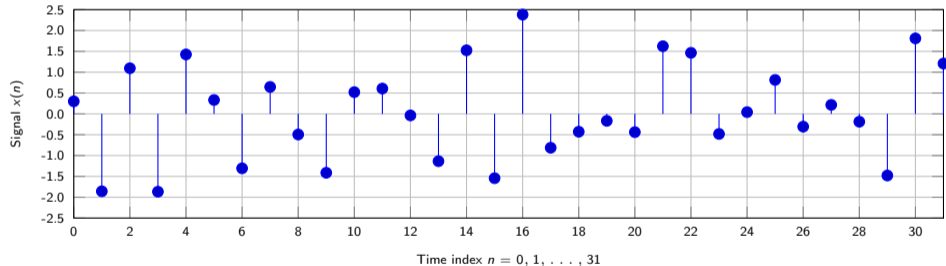
⇒ Dimensionality ⇒ The number of possible signals is too large



- ▶ There are 10^{16} signals that we can generate with 16 components

- ▶ What is so difficult about signal processing?

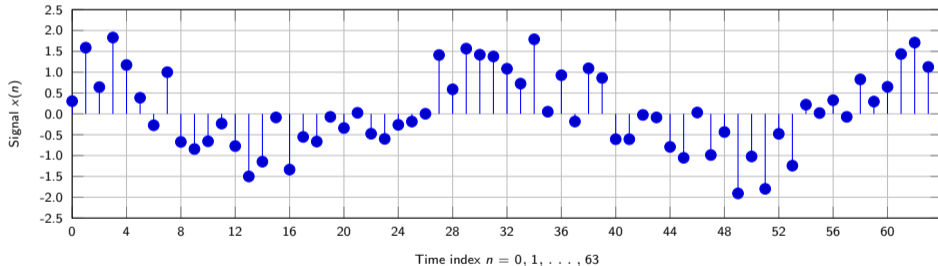
⇒ Dimensionality ⇒ The number of possible signals is too large



- ▶ There are 10^{32} signals that we can generate with 32 components

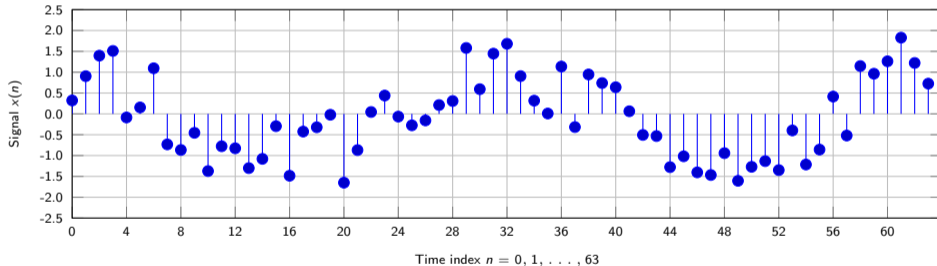
- ▶ What is so difficult about signal processing?

⇒ Dimensionality ⇒ The number of possible signals is too large



- ▶ There are 10^{64} signals that we can generate with 64 components

- ▶ What is so difficult about signal processing?
 - ⇒ Dimensionality ⇒ The number of possible signals is too large

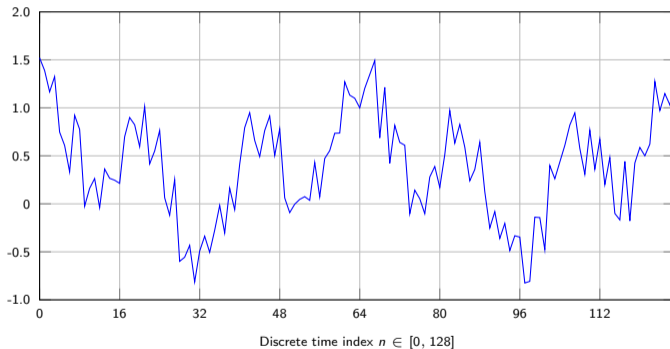


- ▶ Let's stop. There are 10^{78} to 10^{82} atoms in the universe

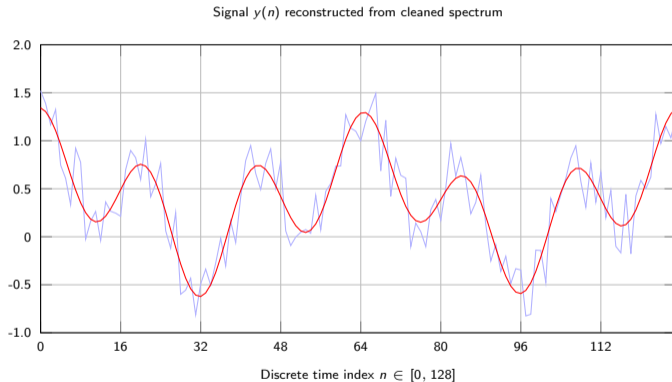
- ▶ Impossible to explore any large dimensional space with any meaningful degree of accuracy.
- ▶ Data points are like the stars in the sky \Rightarrow A lot. But far between.
- ▶ And yet, our eyes can identify patterns with so much ease...

- ▶ When you look at this signal **ALL of you can tell me what it is**

Original signal $x(n)$. It moves randomly, but not that much



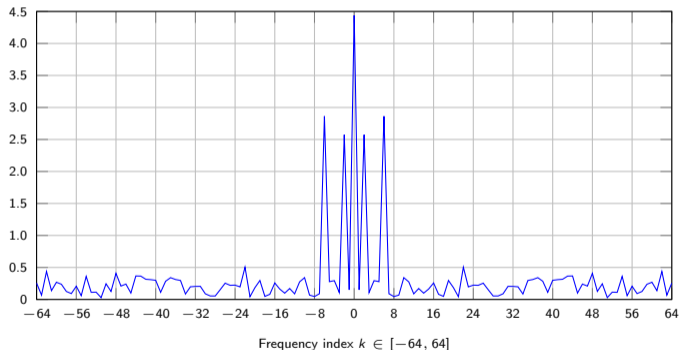
- ▶ When you look at this signal **ALL of you can tell me what it is**



- ▶ **The slow oscillation is a pattern.** **The fast oscillation is noise**

- ▶ We represent the signal in the frequency domain.
 - ⇒ We decompose into different modes of variability (slow and fast)

DFT $X(k)$ of original signal

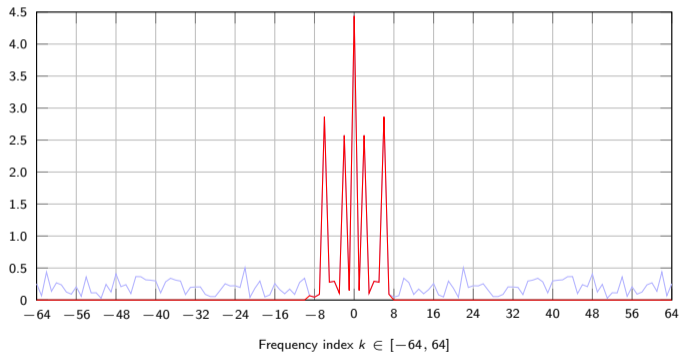


- ▶ The pattern (spikes) is clearly separated from the noise (the floor)

- ▶ We represent the signal in the frequency domain.

⇒ We decompose into different modes of variability (slow and fast)

DFT $Y(k)$ of signal with reshaped spectrum



- ▶ Keep the pattern. Remove the noise

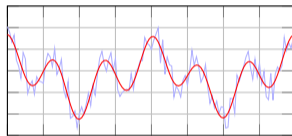
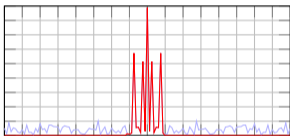
- ▶ The Fourier transform is an **alternative representation** of the signal
- ▶ It is equivalent \Rightarrow Can go back and forth. **Information is preserved**
- ▶ But patterns are easier to explain \Rightarrow **Information is uncovered**
- ▶ Fourier representation is called frequency (variability) representation
- ▶ Literally a **new sense** to view things that are otherwise invisible

*“On ne voit bien qu’avec le **coeur**.
L’essentiel est invisible pour les yeux.”*

The Little Prince

- ▶ **Coeur** being, of course, the french word for **frequency**

- ▶ This does work. This is how I generated the red (clean) signal



- ▶ Don't have to undo transformation \Rightarrow Except for the benefit of our eyes

- ▶ Indeed. If you are not in awe, you don't have a heart.
 - ⇒ Change majors. We don't want you here.
 - ⇒ Just kidding! Stay here, and let me convince you!
- ▶ But magic is not real magic ⇒ It's a trick the magician can explain
- ▶ The Fourier transform reduces the dimensionality of the problem
 - ⇒ There are only a few Fourier coefficients that are meaningful
 - ⇒ These are not stars in the sky anymore
 - ⇒ The Fourier transform concentrates information

- ▶ Frequency representations is how we uncover patterns in time signals
⇒ Noise removal. Compression. Speech recognition.
- ▶ Images ⇒ Two (multi) dimensional Fourier transforms
- ▶ Random Signals ⇒ Principal Component Analysis
- ▶ Signals with arbitrary structures ⇒ Graph Signal Processing

- ▶ We talk representations and their role in concentrating information
 - ⇒ But we don't dwell too much on how to **exploit** representations
- ▶ ESE 305 Foundations of Data Science
- ▶ ESE 545 Data Mining: Learning from Massive Datasets
- ▶ CIS 520 Machine Learning
- ▶ Deep Learning ⇒ Convolutional Neural Networks (CNNs)
 - ⇒ Fourier transforms and Convolutional filters are equivalent
 - ⇒ CNNs compose convolutional filters with local nonlinearities
- ▶ Graph Neural Networks ⇒ <https://gnn.seas.upenn.edu>